# Feature Selection in Evolved Artificial Neural Networks using the Evolutionary Algorithm EPNet

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# Abstract

The evolution of Artificial Neural Networks (ANNs) using the EPNet algorithm has given good results in previous publications. However, the input feature selection problem has never been fully considered before, because the inputs were fixed and only the architectures evolved. Thus, in this work is presented an empirical study to determine statistically whether it is better (or not) to evolve the inputs for the EPNet algorithm. To test this, a prediction task was used with 21 Time Series from different dynamics and fields. The results obtained show that the evolution of inputs does improve the performance of the algorithm in some cases, but leads to worse performance in others.

## 1 Introduction

In previous studies with the EPNet algorithm [11, 12] the user set manually the required number of inputs and then evolved the ANN architectures. In this sense, no input feature selection technique has been used in the EPNet algorithm. Instead, existing domain knowledge was used to chose appropriate inputs before the evolution of the ANNs began, i.e. the input units were fixed throughout the evolution.

Elsewhere, feature selection techniques have proved useful because there is always the possibility of presenting redundant or irrelevant inputs to the ANNs, e.g. the information given by them could already be presented in other input units, or they could simply not contribute to solving the problem. Thus, if the information is redundant, it will add nothing to solving the task, and if it is irrelevant, it will not improve the results [3]. Moreover, if input feature selection is not used, it is possible that unnecessary inputs will result in bigger ANNs requiring more time in the training process, or introduce unnecJohn A. Bullinaria School of Computer Science University of Birmingham Birmingham, B15 2TT UK J.A.Bullinaria@cs.bham.ac.uk

essary noise into the ANN which will typically result in poorer ANN output performance.

Existing feature selection techniques fall into two general categories [3]: *Generational* procedures and *Evaluation function* procedures. In both methods, several different variations are used to determine what are the most appropriate inputs to the model.

In this work it was decided to not use an *Evaluation functions* method to determine appropriate inputs, because this procedure adds an extra stage in the solution of the task, i.e. first an appropriate number of inputs has to be determined, and only then is the main procedure applied to solve the problem [5, 8, 9, 14]. This approach has previously been applied to forecasting [5, 8] and to classification [9, 14].

Consequently, the approach adopted in this work belongs to the *Generational* procedures, because it evolves the ANNs' inputs with an Evolutionary Algorithm (EA) [2, 7] to allow the automatic adaptation of the inputs at the same time as the rest of the architecture evolves.

Since the EPNet algorithm is based on the Evolutionary Programming approach, it only uses mutations to perform the evolution. Therefore, it avoids the well-known evolutionary ANN permutation problem that can arise with crossover operators [11]. Thus, by applying a feature selection technique over the EPNet algorithm, one can have better confidence in the results than if it is applied over an algorithm that is not so good for this task, such as a Genetic Algorithm (GA).

In the literature it is possible to find several approaches and combinations of them to solve diverse kinds of problems using feature selection, e.g. leaving the architectures fixed and finding appropriate inputs [4, 9], or leaving the inputs fixed and then evolving the ANNs' architectures [6, 11, 12] to adapt the networks to the inputs. In this work a more general approach is adopted, in which both aspects are evolved (inputs and architectures). Thus, for this study were performed a series of experiments to determine the sensitivity of the evolution of inputs in the EPNet algorithm, i.e. it was explored whether it is better or not to evolve the inputs. Since evolving the inputs means that there are more parameters to evolve, this could potentially compromise the performance of the algorithm, and it was important to test if and when that does happen.

The rest of this paper is organized as follows: Sec. 2 presents information regarding the EPNet algorithm and the configurations used to perform the experiments. In Sec. 3 is shown the experimental results of the modified algorithm. Then the conclusions are provided in Sec. 4.

## 2 The Algorithm and Parameters

The EPNet algorithm [13] was developed using Fogel's Evolutionary Programming (EP) approach to evolve small ANN architectures. That was done by implementing five different mutation operators to evolve the architectures and weights learning. Since it is based on EP, it does not use any crossover operators to perform the architecture evolution, thus avoiding the wellknown evolutionary ANN permutation problem [11]. However, the algorithm was not developed to have an input feature selection stage.

The EPNet algorithm has been tested on a diverse set of problems for classification and prediction [13, 12]. In this paper is studied the Time Series (TS) forecasting task. The multiple step prediction approach is used to perform short term prediction (30 steps ahead) for 21 TS of different dynamics. The aim is at time t to predict the TS at future times from past values  $\{x_t, x_{t-1}, x_{t-2}, ...\}$ , and feature selection corresponds to deciding which past values  $\{x_i\}$  to use as the ANN inputs. Typically this is simplified to choosing how many inputs n and what delay d to get the input set  $\{x_t, x_{t-d}, ..., x_{t-(n-1)d}\}$ , but more complex choices are possible.

To measure the performance of the evolved ANNs, the Normalized Root Mean Squared Error (NRMSE) on previously unseen test sets is used, which is known to be a robust metric to validate TS prediction results.

In previous studies with the EPNet algorithm, only a small number of generations were used to obtain the best evolved individual, e.g. [13] used only 200 generations. Here, to fully test the evolutionary process and behavior of the algorithm, 2000 generations are used.

Two cases, described next, are compared: first the control case where ANNs are evolved with fixed inputs (as in the original EPNet algorithm), and then the feature selection case with everything else the same except that the inputs are evolved within the EPNet algorithm.

#### 2.1 Fixed Inputs

For the fixed input case, a feature selection approach is needed to determine an appropriate fixed number of inputs and associated delays before the evolutionary process begins. Here was employed the Takens embedding theorem that has been used before for the TS prediction task [10]. With this, the number of inputs is chosen with the False Nearest Neighbour method, and the delays between them are fixed using the Average Mutual Information. Both techniques were obtained and applied from [1].

There are other studies that have used these methods, such as [4], but these did not evolve the ANNs and instead used fixed architectures to predict the Lorenz TS.

#### 2.2 Feature Selection in the EPNet

As explained above, the *Evaluation function* approach was not chosen because the selection of inputs is then a separate process from the evolution of the ANNs. Rather, it is natural that everything should be evolved at the same time, allowing the inputs to adapt as required.

To avoid introducing complex and unnecessary new operators for evolving the inputs, they were evolved inside the EPNet using the same operators already developed for the original algorithm, i.e. the inputs were simply treated in the same way as any other node in the ANN. There are a series of potential input nodes corresponding to the TS at past times, i.e.  $\{x_t, x_{t-1}, x_{t-2}, ...\}$ , and the add/delete node mutation process selects which subset are actually used in the network. Unlike in the fixed inputs case, the *n* chosen inputs will not necessarily be separated by some fixed time delay *d*.

#### **3** Experimental Results

In this section is presented the results of the experiments designed to determine whether it is better, or not, to evolve the ANN inputs.

Each evolutionary experiment was repeated 30 times to allow a reliable statistical analysis of the results. After each evolutionary run had finished, the best individual evolved was identified by measuring the NRMSE on an independent test set, and the NRMSE, inputs, hidden nodes

Table 1: Effect of evolving inputs instead of using fixed inputs, showing counts out of 21 TS after 2000 generations of evolution

	NRMSE	Inputs	Hidden	Cons
Lower mean	13	13	6	11
Lower at 0.05 sig.	11	13	2	8
Higher mean	8	8	15	10
Higher at 0.05 sig.	6	8	7	8

and connections were recorded for performing the comparisons.

Table 1 summarizes the results of the comparisons showing how many of the 21 TS have significant changes for each variable if the inputs are evolved rather than fixed. The comparison is made for the NRMSE, and the numbers of inputs, hidden nodes and connections, from the best individuals found over 30 independent runs. Row *Lower Mean* indicates how many TS have lower mean values over 30 runs for each variable presented, and row *Lower at* 0.05 *sig.* shows how many are lower at 0.05 level of significance using a *t-test* (two-tailed with unequal variances). Similarly, row *Higher mean* and *Higher at* 0.05 *sig.* indicate how many TS have higher values.

Thus 11 TS achieve significantly smaller errors on the predictions (NRMSE) by evolving the inputs, 6 TS were significantly better if the inputs were fixed, leaving 4 TS with no significant difference. The Inputs column shows that the evolution of inputs allows significantly smaller numbers of ANN inputs for 13 TS, but significantly larger numbers for 8 TS. Looking at the hidden nodes, significantly smaller networks emerged in 7 TS if the inputs were fixed, compared with only 2 TS if the inputs are evolved, maybe because for fixed inputs the EPNet algorithm has fewer parameters to evolve, and consequently has more options to find networks with fewer hidden nodes. Regarding the number of connections, the evolved ANNs for 8 TS have significantly more, while 8 have significantly less, when the inputs are evolved.

If the evolution is stopped at much smaller numbers of generations (i.e. far fewer than 2000, as in most previous studies), the average NRMSE and network sizes tend to be larger, indicating that the networks are still evolving and that the best possible results have not yet been achieved.

The results presented in Table 1 show that, overall, evolving the inputs with the EPNet algorithm leads to better TS prediction (i.e. lower

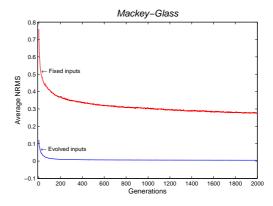


Figure 1: Average NRMSE for the Mackey-Glass TS with fixed and evolved inputs

NRMSE) with networks of similar sizes. However, the results are mixed, and to fully understand the benefits, or otherwise, of evolving the inputs, one needs to look more carefully at what emerges for the individual TS.

Table 2 presents the number of evolved inputs found after 2000 generations (columns 2-5), the fixed number of inputs found with the False Nearest Neighbours method (column 6) and the delays found using the Average Mutual Information (column 7). Here is not presented the delays found with the evolutionary algorithm because many complex variations are possible. For example, if ten inputs are available  $\{x_t, ..., x_{t-9}\}$ , three fixed inputs with a delay of 2 means using  $\{x_t, x_{t-2}, x_{t-4}\}$ , but if the inputs are evolved, more complex selections could emerge, such as  $\{x_t, x_{t-5}, x_{t-7}\}$  or  $\{x_{t-4}, x_{t-7}, x_{t-8}\}$ .

A clear example of this issue arises with the Henon TS. Table 4 shows that the best evolved network in this case has 7 inputs, which are  $\{x_t, x_{t-1}, x_{t-3}, x_{t-5}, x_{t-9}, x_{t-15}, x_{t-16}\}$ , in which the delays between inputs are unequal. If the inputs are fixed, the False Nearest Neighbour method gives a value of 5 and the Average Mutual Information gives a delay of 9 (Table 2), which corresponds to having the input vector  $\{x_t, x_{t-9}, x_{t-18}, x_{t-27}, x_{t-36}\}$ .

Even though there are more parameters to evolve if the inputs are not fixed, the algorithm can still obtain faster results in some cases. For example, in Fig. 1 is shown the average NRMSE over the entire evolution, with fixed and evolved inputs, for the Mackey-Glass TS. It can be seen that the evolution of inputs allows the algorithm to obtain smaller errors faster (particularly at the beginning of the evolution). Conversely, there were other cases where the error was reduced faster if the inputs were fixed, for example the QP2, QP3, Rossler, Star and D1 TS.

Time Series		Evolution o	$Fixed \ values$			
1 ime Series	Mean	$Std \ Dev$	Min	Max	Inputs	Delays
Henon	10.23	2.800041	5	16	5	9
Ikeda	11.57	2.329471	6	16	7	5
Logistic	12.40	2.190890	7	16	3	9
Lorenz	12.63	2.189053	9	17	5	17
Mackey-Glass	12.47	1.995397	8	17	19	19
Qp2	12.67	1.625939	10	16	7	22
Qp3	11.63	1.629117	7	15	9	6
Rossler	11.10	1.936046	6	14	13	12
Births in Quebec	11.20	2.074475	5	14	21	4
Dow Jones	11.50	1.943158	8	16	21	46
Gold Prices	11.40	2.206573	8	16	21	27
IBM Stock	12.27	2.016028	6	17	19	52
SP500	12.07	2.273283	6	16	21	25
Colorado River	11.10	2.564344	5	16	13	3
Lake Eriel	11.13	2.255007	5	15	17	7
Equipment Temp.	11.17	2.780267	5	17	17	33
Kobe	11.83	2.290661	8	16	5	4
Star	13.10	2.171127	10	17	5	6
Sunspot	11.33	1.971055	7	16	19	23
D1	10.93	2.504249	6	15	21	8
Laser	13.10	1.647359	9	17	19	2

Table 2: Evolved inputs versus fixed inputs in the EPNet algorithm with 2000 generations

In Tables 3 and 4 are presented the NRMSE and network sizes for the fixed and evolved inputs respectively. It is these results that were summarized in Table 1. Columns 2-5 give the mean, standard deviation, minimum and maximum values of the NRMSE (evaluated on previously unseen test sets) for the best individuals from the 30 runs. Columns 6-8 give the number of inputs, hidden nodes and connections of the best individuals overall from the 30 runs, corresponding to the NRMSE in column Min.

Comparing the results for individual TS, there are no obvious patterns indicating why evolved inputs provide better NRMSE performance in some cases but not others. Although evolving the inputs means more parameters to evolve, the EPNet algorithm still finds smaller architectures for some TS, though larger architectures are found for others. Moreover, there appears to be no correlation between the cases of improved performance and any of the other differences that emerge as a result of having evolved rather than fixed inputs.

For example, if the size of an ANN is taken to be the total number of trainable connections, then out of the 11 TS improved at 0.05 level of significance for the NRMSE, only 6 TS obtain smaller architectures for the best individual found than when the inputs are fixed (Connections columns in Tables 4 and 3). These TS are Mackey-Glass, Dow Jones, Gold Prices, Colorado River, Lake Eriel and Laser. For the 8 TS that were better if the inputs are fixed, only QP2, QP3 and IBM Stock had smaller architectures than if the inputs are evolved.

## 4 Conclusions

This paper studied the issue of feature selection for evolved ANNs. It presented a series of experiments to determine whether it is better, or not, to evolve the inputs when the EPNet algorithm is used for TS prediction tasks. This was done by comparing evolving the inputs against keeping them at fixed computed values throughout the evolutionary process. The fixed inputs were computed using the approaches employed in previous studies, namely False Nearest Neighbour for the number of inputs and Average Mutual Information for their delays.

It was shown that evolving the inputs gave significantly better prediction results for 11 of the 21 TS studied, but in 6 cases was it better to keep the inputs fixed. For the remaining 4 TS there was no significant difference. This led to the conclusion that it is certainly not the

Table 3: Individual TS results for fixed inputs. Evolved NRMSE and architecture parameters for the best individual values over 30 runs with 2000 generations

Time Series	NRMSE				Best Ind.		
	Mean	$Std \ Dev$	Min	Max	Inputs	Hidden	Connections
Henon	0.785112	0.103130	0.552615	0.981666	5	14	131
Ikeda	0.959694	0.034274	0.849187	1.014560	7	14	144
Logistic	0.001052	0.000652	0.000217	0.002870	3	11	71
Lorenz	0.016993	0.009701	0.004919	0.047069	5	15	138
Mackey-Glass	0.336494	0.035695	0.259019	0.415552	19	10	176
$_{\rm Qp2}$	0.028665	0.006725	0.016584	0.043588	7	14	147
Qp3	0.176651	0.055778	0.093578	0.325843	9	12	128
Rossler	0.142443	0.247063	0.001809	1.118090	13	12	157
Births in Quebec	0.516288	0.029663	0.440343	0.586517	21	8	131
Dow Jones	1.409703	0.329013	0.744604	2.041210	21	9	178
Gold Prices	1.305383	0.415891	0.710825	2.427460	21	15	308
IBM Stock	0.715871	0.112638	0.459090	0.996211	19	12	200
SP500	0.597546	0.067702	0.444256	0.768787	21	15	288
Colorado River	0.964563	0.079263	0.844041	1.139390	13	15	223
Lake Eriel	0.770567	0.246672	0.425295	1.457200	17	9	140
Equipment Temp.	0.683046	0.173931	0.296670	1.207780	17	16	278
Kobe	1.009605	0.145755	0.668835	1.329590	5	16	153
Star	0.025598	0.004490	0.015847	0.036367	5	13	115
Sunspot	0.539722	0.110897	0.371779	0.897257	19	17	322
D1	1.030869	0.216930	0.569237	1.429940	21	14	272
Laser	0.153638	0.045795	0.088370	0.320004	19	14	268

Table 4: Individual TS results for evolved inputs. Evolved NRMSE and architecture parameters for the best individual values over 30 runs with 2000 generations

Time Series	NRMSE				Best Ind.			
	Mean	$Std \ Dev$	Min	Max	Inputs	Hidden	Connections	
Henon	0.654182	0.197501	0.336084	1.038330	7	12	114	
Ikeda	0.905389	0.061768	0.653851	0.991480	15	17	283	
Logistic	0.000592	0.000378	0.000126	0.001495	12	15	192	
Lorenz	0.019564	0.011186	0.003145	0.044841	17	16	290	
Mackey-Glass	0.004186	0.002008	0.001673	0.012219	12	12	164	
$_{\rm Qp2}$	0.071087	0.036165	0.025993	0.193532	13	17	258	
Qp3	0.404328	0.120893	0.149107	0.630460	11	15	204	
Rossler	0.005333	0.017721	0.000506	0.097060	11	17	242	
Births in Quebec	0.513337	0.017996	0.465915	0.545526	12	19	306	
Dow Jones	1.097907	0.053064	0.997859	1.211680	11	12	155	
Gold Prices	1.057707	0.151929	0.835188	1.532440	14	14	205	
IBM Stock	0.875539	0.062092	0.745606	0.995658	13	18	279	
SP500	0.648791	0.025466	0.590659	0.706523	11	12	157	
Colorado River	0.802570	0.090089	0.600033	0.968082	8	15	182	
Lake Eriel	0.704184	0.103292	0.395519	0.920900	13	8	95	
Equipment Temp.	0.784072	0.088246	0.604829	0.939192	11	13	157	
Kobe	0.808204	0.145650	0.543781	1.166810	11	15	192	
Star	0.022751	0.005533	0.013487	0.033852	17	14	245	
Sunspot	0.670356	0.100118	0.446804	0.873600	10	9	93	
D1	1.089576	0.216749	0.714094	1.525940	14	13	202	
Laser	0.060268	0.018450	0.026656	0.091397	14	17	263	

case that using the values given by the False Nearest Neighbour and Average Mutual Information is the best way to perform input feature selection, i.e. to fix the inputs during the evolutionary process. However, one can also conclude that the standard EPNet algorithm is not capable of finding the best input features in all cases either. Moreover, looking at the detailed results for individual TS did not reveal any clear picture of when evolving the inputs would be better.

Since it should in principle be possible for the evolution of the inputs to find the computed inputs used in the fixed input case, one needs to ask why the EPNet algorithm is not finding them in the cases where they lead to better performance than the actual evolved inputs. One possibility is that the evolution simply needs to be run for even more generations, and that is something that clearly needs to be explored further. Another issue is that the mutation operations of adding or deleting random inputs introduce a lot of noise into the operation of the evolving ANNs, and for some TS that is clearly leading to worse performance than if the inputs are fixed. This suggests two more strands for taking this research further: first looking more carefully at the disruption caused by the changes to the inputs during evolution, and second looking at making the evolution of inputs easier by starting at the computed values so that evolution can improve on them where possible, but hopefully not end up with inferior values. By following these ideas it is hoped that simple extensions to the evolutionary ANN approach presented in this paper will result in improved feature selection and resultant performance in many cases, and worse performance in none.

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